The Dynamic Stark-Effect in a Turbulent Hydrogen Plasma

W. R. Rutgers and H. de Kluiver

Association Euratom-FOM, FOM-Instituut voor Plasmafysica, Rijnhuizen, Jutphaas, The Netherlands

(Z. Naturforsch. 29 a, 42-44 [1974]; received October 22, 1973)

The profiles of the first three Balmer lines of hydrogen are measured in a turbulent heating experiment. From the position of Stark satellites the field strength of low frequency oscillations $(\omega \sim \omega_{\rm pl})$ is calculated. The energy density in these electrostatic oscillations can amount to 1% of the thermal energy. The presence of high frequency oscillations $(\omega \sim \omega_{\rm pe})$ is concluded from satellites near $\pm \omega_{\rm pe}$ from the unperturbed line position.

In turbulent heating experiments an electric field exceeding the run-away field, is applied to a plasma. This results in the excitation of e-e and e-i two-stream instabilities and ion-acoustic instabilities leading to a high level of longitudinal electrostatic oscillations. The wave energy saturates by the interaction between waves and particles. The transfer of energy from the waves to particles lead to electron and ion heating. In this paper the effect of low frequency ion oscillations ($\omega \sim \omega_{\rm pi}$) and high frequency electron oscillation $(\omega \sim \omega_{\rm pe})$ on the line shape of hydrogen spectral lines is shown experimentally. The observation of the profiles of the Balmer series can yield important information on the microscopic electric fields during the turbulent stage 1.

Calculations for the Ly_{α} line have been reported by Cohn et alias ². Similar calculation for the H_{α} and H_{β} profile under influence of static and dynamic fields are under way.

The turbulent plasma is produced by the discharge of a capacitor $(2 \,\mu\text{F}, \, 15-40 \,\text{kV})$ across a hollow cathode discharge in a strong magnetic field $(B=0.4-2 \,\text{T}, \, \text{discharge length} \, 0.8 \,\text{m})$. The profiles of the Balmer lines H_a , H_β , and H_γ are scanned with a one meter MacPherson monochromator in steps of $1/3 \,\text{Å}$. The spectra are time averages over $0.5 \,\mu\text{sec}$ from three successive shots while the turbulent stage lasts for about $3 \,\mu\text{sec}$. Side-on observations are carried out with a polarizer between plasma and monochromator. Specimens of the H_β and H_α lines are given in Figs. 1 and 2.

It is known from probe ³ and radiation ⁴ measurements that electrostatic oscillations at frequencies below $\omega \sim 2~\omega_{\rm pi}$ are present during turbulent heating. Besides that, strong electron oscillations at

Reprint requests to Drs. W. R. Rutgers, FOM-Instituut voor Plasmafysica, Rijnhuizen, Postbus 7, Jutphaas.

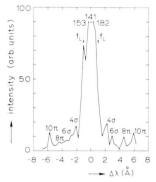


Fig. 1. Measured profile of the H_{β} line for $t=1-1.5~\mu{\rm sec.}$ $f_{\rm L}$ indicates the satellites caused by Langmuir oscillations. The parameter $\delta_{\rm S}$ is greater than 100 for the Stark components $4~\sigma$, $6~\sigma$, $8~\pi$ and $10~\pi$.

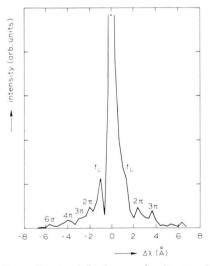


Fig. 2. H_a profile. $t=1.5-2~\mu{\rm sec}$, density $n=10^{20}~{\rm m}^{-3}$. The electric field applied to the plasma is $E_0=28~{\rm kV~m}^{-1}$. The electric field $\tilde{E}\!=\!E_{\rm S}$, deduced from the separation of the Stark components is 3.6 MV m⁻¹.

 $\omega \sim \omega_{\rm pe}$ were found ⁵. The influence of low frequency fields on individual Stark components is in-



Dieses Werk wurde im Jahr 2013 vom Verlag Zeitschrift für Naturforschung in Zusammenarbeit mit der Max-Planck-Gesellschaft zur Förderung der Wissenschaften e.V. digitalisiert und unter folgender Lizenz veröffentlicht: Creative Commons Namensnennung-Keine Bearbeitung 3.0 Deutschland

This work has been digitalized and published in 2013 by Verlag Zeitschrift für Naturforschung in cooperation with the Max Planck Society for the Advancement of Science under a Creative Commons Attribution-NoDerivs 3.0 Germany License. vestigated by Yakovlev ⁶. He calculated the line shape in a harmonic electric field $\mathbf{E}_{\mathrm{S}}(t) = \mathbf{E}_{\mathrm{S}} \sin{(\Omega_{\mathrm{S}}\,t + \varphi)}$ for random phase φ in the quasi stationary limit $\delta_{\mathrm{S}} = \Delta\Omega_{\mathrm{S}}/\Omega_{\mathrm{S}} \gg 1$. $\Delta\Omega_{\mathrm{S}}$ is the shift due to a field $|\mathbf{E}_{\mathrm{S}}|$ and Ω_{S} the angular frequency. His calculation results in a sharp maximum in the radiation intensity near the position of the Stark satellite for completely static fields of the same value. It is known ⁷ that high frequency fields $\mathbf{E}_{\mathrm{D}}\sin{\Omega_{\mathrm{D}}\,t}$ ($\delta_{\mathrm{D}} = \Delta\Omega_{\mathrm{D}}/\Omega_{\mathrm{D}} \lesssim 1$) only give rise to satellites at $\pm n\,\Omega_{\mathrm{D}}$ with n an integer.

Here the composite electric field may be described by

$$\mathbf{E} = \mathbf{E}_{\mathrm{S}}\cos\left(\Omega_{\mathrm{S}}t + \varphi\right) + \mathbf{E}_{\mathrm{D}}\cos\left(\Omega_{\mathrm{D}}t + \varphi_{2}\right)$$

during some tens of ion plasma periods. For the experimental density of about $10^{20}\,\mathrm{m}^{-3}$ the fundamental frequencies are $\Omega_\mathrm{S}\sim 10^{10}\,\mathrm{sec}^{-1}$ and $\Omega_\mathrm{D}\sim 5\cdot 10^{11}\,\mathrm{sec}^{-1}$. Rough estimates for $\Delta\Omega_\mathrm{S}$ and $\Delta\Omega_\mathrm{D}$ can be obtained from anomalous conductivity data and from the emitted radiation near ω_pe^{-5} . From this follows $\delta_\mathrm{S}\!>\!50$ and $\delta_\mathrm{D}\!<\!1$ for our experimental conditions. The high frequency field gives satellites at the Langmuir frequency, f_L , and harmonics, symmetrically with respect to the unshifted line and the quasi-static Stark components.

The measured H_β profile (Fig. 1) and H_α profile (Fig. 2) show satellites at f_L during the entire turbulent state whereas separate Stark components

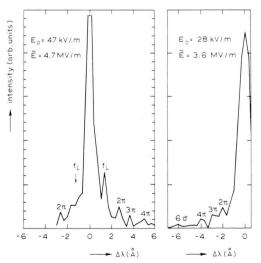


Fig. 3. The H_{α} profile for two values of the applied field E_0 . Plasma conditions see Figure 2.

analysed as 4σ , 6σ , 8π , and 10π for H_{β} and 2π , 8π , 4π and 6σ for H_{α} appear after 0.5 μ sec. The frequency shift of the distinct Stark components is larger than $10^{12}\,{\rm sec}^{-1}$. The intensities seem to be correlated with ion heating 8 . In Fig. 3 the H_{α} profile is shown for two different values of the electric field across the discharge. The turbulent fluctuations increase with increasing applied field, as is found from the separation of the Stark components. Measured values of the electrostatic field strength $\tilde{E}=E_{\rm S}$ are given in Table 1.

Table 1. Measured values of the field strength $\tilde{E} = E_s$ of the low-frequency electrostatic oscillations.

| line | Orientation of polarizer | Applied field E_0 | |
|----------------------------------|--------------------------|--------------------------------|-----------------------------------|
| $\overline{\mathrm{H}_{\alpha}}$ | | $47 	imes 10^3 \ \mathrm{V/m}$ | $4.5	imes10^6~\mathrm{V/m}$ |
| H_{α} | | 47 | 4.7 |
| H_{β} | Ï | 47 | 4.5 |
| H_{α} | Ï | $28 	imes 10^3 \mathrm{V/m}$ | $3.6 \times 10^6 \; \mathrm{V/m}$ |
| H_{α} | 1 | 28 | 3.6 |
| H_{β} | Ï | 28 | 3.5 |
| ${ m H}_{\gamma}$ | Ï | $25 	imes 10^3 \ V/m$ | $3.2 	imes 10^6 \mathrm{V/m}$ |

Earlier observations of the H_{β} side bands have been reported at the V European Conference 9 but at that time the spectral resolution was insufficient to see the individual Stark component resolved. Gallagher and Levine 10 have reported Balmer line anomalies of the same character for a toroidal high- β plasma. The relation between shift and field strength for the components $k \, \pi$ and $k \, \sigma$ is $\Delta \Omega = 3/2 \, a_0 \, k \, E_{\rm S}$.

The intensities of the π and σ components are rather insensitive for the orientation of the polarizer between plasma and monochromator. This indicates that the low frequency electrostatic waves have no preferential direction of propagation for this particular experiment.

Acknowledgement

The authors are indebted to Prof. C. M. Braams for fruitful discussions.

The help of Mr. R. A. A. Ambags and Mr. B. de Groot during the measurements and the acquisition of the data is greatly appreciated.

This work was performed under the Euratom-FOM association agreement with financial support from ZWO and Euratom.

¹ A. B. Berezin et al., Sov. Phys.-Tech. Phys. 17, 750 [1972].

² A. Cohn, P. Bakshi, and G. Kalman, Phys. Rev. Letters

29, 324 [1972].

³ S. M. Hamberger and J. Jancarik, Phys. Fluids 15, 825 [1972]; K. Adati et al., Proc. Sixth European Conf. on Contr. Fusion and Plasma Physics, Vol. 1, Moscow 1973,

⁴ W. R. Rutgers, Phys. Letters **40 A**, 99 [1972].

- ⁵ H. Schrijver, accepted for publication in Physica. Yu. G. Kalinin et al., Sov. Phys.-JETP 28, 61 [1969].
- ⁶ D. G. Yakovlev, Sov. Phys. Tech. Phys. 17, 1248 [1973].
 ⁷ D. Blokhintsev, Phys. Z. Sowjet Union 4, 501 [1933].; M. Barranger and B. Moser, Phys. Rev. 123, 25 [1961].

⁸ H. W. Piekaar, Plasma Physics **15**, 565 [1973].

- H. W. Piekaar et al., Proc. Fifth European Conf. on Contr. Fusion and Plasma Physics, Vol. 1, Grenoble 1972, p. 147.
- 10 C. C. Gallagher and M. A. Levine, Phys. Rev. Letters 30, 897 [1973].